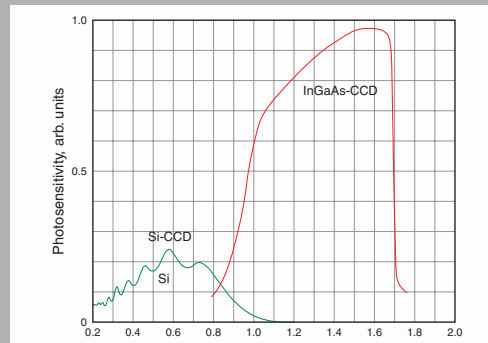


**Abstract:** We report on the first observation of the nonlinear cascading  $\chi^{(3)} \leftrightarrow \chi^{(3)}$  effects in UV spectral range and second harmonic generation stipulated by the “defect” nonlinearity under one-micron pumping in crystalline ceramics based on cubic oxides  $\text{Sc}_2\text{O}_3$  and  $\text{Lu}_2\text{O}_3$ . Broadband their multi-wavelength Stokes and anti-Stokes combs with the extension of  $10475 \text{ cm}^{-1}$  (for  $\text{Sc}_2\text{O}_3$ ) and  $8232 \text{ cm}^{-1}$  (for  $\text{Lu}_2\text{O}_3$ ) were recorded as well.



Spectral sensitivity of Si- and InGaAs-CCD linear image sensors S3923-1024Q and G9204-512D, respectively

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# New nonlinear-laser effects in crystalline fine-grained ceramics based on cubic $\text{Sc}_2\text{O}_3$ and $\text{Lu}_2\text{O}_3$ oxides: second and third harmonic generation, and cascaded self-sum-frequency mixing in UV spectral region

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**Key words:** nonlinear-laser effect; laser cascading; stimulated Raman scattering; SHG; THG; Stokes and anti-Stokes comb;  $\text{Sc}_2\text{O}_3$  and  $\text{Lu}_2\text{O}_3$  ceramics

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## 1. Introduction

In last decade modern crystalline gain materials doped with lanthanide ( $\text{Ln}^{3+}$ ) lasants are increasingly employed in the ceramic forms. A number of revolutionary fabrication methods have been developed (see, e.g. [1]) to add and replace commonly used crystal growth techniques so that laser ceramics can be obtained a lower cost and larger

size. The constitution of grains and grain boundaries are fundamental difference between the crystalline ceramics and single crystals.

In spite the fact that with these ceramics allowed to get already very impressive advances, e.g. the achievement of about 100 KW output CW power ( ${}^4\text{F}_{3/2} \rightarrow {}^4\text{I}_{11/2}$  channel of  $\text{Nd}^{3+}:\text{Y}_3\text{Al}_5\text{O}_{12}$  ceramic laser [2]) and efficient sub-100 fs ytterbium generation ( ${}^2\text{F}_{5/2} \rightarrow {}^2\text{F}_{7/2}$  lasing

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Ceramics	Space group <sup>a)</sup>	Ln <sup>3+</sup> lasant	Nonlinear effect	$g_{ssR}^{St1}$ <sup>b)</sup> cm/GW
Sc <sub>2</sub> O <sub>3</sub>	$T_h^7$	Yb <sup>3+</sup>	SRS, SHG, THG, self-SFM(SRS) <sup>c)</sup>	≈ 0.72 [8]
Y <sub>2</sub> O <sub>3</sub>	$T_h^7$	Nd <sup>3+</sup> , Yb <sup>3+</sup>	SRS	≈ 0.4 [9]
Y <sub>3</sub> Al <sub>5</sub> O <sub>12</sub>	$O_h^{10}$	Nd <sup>3+</sup> , Er <sup>3+</sup> , Yb <sup>3+</sup>	SRS	≈ 0.1 [9–11]
Ba(Sn,Zr,Mg,Ta)O <sub>3</sub> (E-type) <sup>d)</sup>	$O_h^5$	–	SRS	≈ 0.15 [12]
Ba(Sn,Zr,Mg,Ta)O <sub>3</sub> (Z-type) <sup>d)</sup>	$O_h^5$	–	SRS	≈ 0.15 [12]
Lu <sub>2</sub> O <sub>3</sub>	$T_h^7$	Nd <sup>3+</sup> , Yb <sup>3+</sup>	SRS, SHG, THG, self-SFM(SRS) <sup>c)</sup>	≈ 0.3 [13]

<sup>a)</sup> Grains of the ceramics are randomly oriented nano- or micro-size single crystals.

<sup>b)</sup>  $g_{ssR}^{St1}$  is the steady-state Raman gain coefficient for first Stokes lasing component measured under one-micron pumping radiation from picosecond Nd<sup>3+</sup>:Y<sub>3</sub>Al<sub>5</sub>O<sub>12</sub> laser.

<sup>c)</sup> Self-SFM(SRS), i.e. self-sum frequency mixing of the arising SRS lasing components and pumping generation.

<sup>d)</sup> In microcrystalline grains of the Ba(Sn,Zr,Mg,Ta)O<sub>3</sub> ceramics the B' and B'' octahedral sites statistically occupy by four unlike valency cations Mg<sup>2+</sup>, Sn<sup>4+</sup>, Zr<sup>4+</sup>, and Ta<sup>5+</sup>, i.e. in this materials is realized the second low of crystal-field disorder [14].

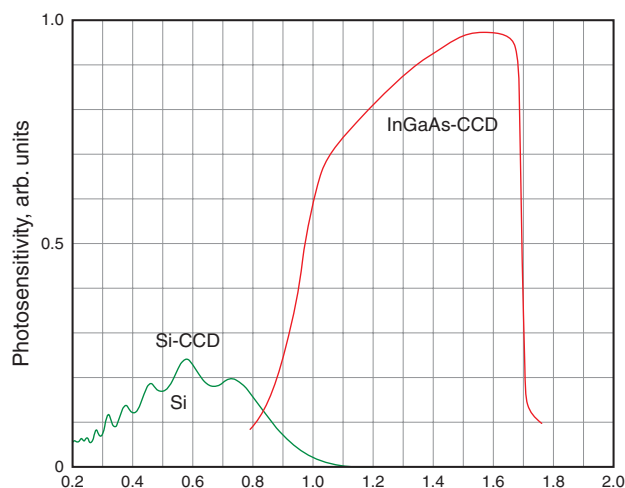
**Table 1** Nonlinear-laser effects in highly-transparent “cubic” ceramics

in Y<sub>2</sub>O<sub>3</sub> and Sc<sub>2</sub>O<sub>3</sub> ceramics [3,4]), many their physical properties need more comprehensive investigation.

In the first place this concerns the grain boundary properties which play a key role in the determination of main characteristics of crystalline laser ceramics and different types of laser on their basis. Recently, it was found that the grain boundaries in these laser-host ceramics improved mechanical toughness and micro-hardness to the same name laser-host crystals [5]. Comparative experiments with the same names of laser single crystals and ceramics have shown that grain boundaries in the latter do not contribute to reducing the optical damage limit [6]. Review paper on the influence of the grain boundaries on the heat transfer in laser ceramics on the base of cubic oxides is given in [7]. The walls of micro-size grains in ceramics on the base of oxide, in particular Sc<sub>2</sub>O<sub>3</sub> and Lu<sub>2</sub>O<sub>3</sub>, are surface defects where the centrosymmetric cubic crystallographic nature (their space group is  $T_h^7 - Ia\bar{3}$ ) is broken. Therefore, in these bulk crystalline ceramics with high concentration of grain-boundary walls should be manifested both cubic  $\chi^{(3)}$ - and quadratic  $\chi^{(2)}$ - nonlinearities under high peak-power of laser excitation, as stimulated Raman scattering (SRS), low-intensity non-phase-matched third and second harmonic generation (THG and SHG)), as well as multi-wave parametric mixing processes. The main goal of this work was the discovery of all these possible nonlinear-laser effects under one-micron picosecond pumping in highly-transparent Sc<sub>2</sub>O<sub>3</sub> and Lu<sub>2</sub>O<sub>3</sub> ceramics which were fabricated in Konoshima Chemical Co. Ltd. Incidentally, in this experiments was the task to significant widen of Stokes and anti-Stokes wings in their SRS spectra. The Table 1 summarized of observed nonlinear-laser interactions in crystalline ceramics on the base of cubic oxides.

## 2. Multi-wavelength nonlinear lasing from UV till mid-IR region

For more detail investigation of single-pass Raman induced nonlinear lasing processes in crystalline host-



**Figure 1** (online color at [www.lphys.org](http://www.lphys.org)) Spectral sensitivity of Si- and InGaAs-CCD linear image sensors S3923-1024Q and G9204-512D, respectively (data from Hamamatsu catalog)

ceramics Sc<sub>2</sub>O<sub>3</sub> and Lu<sub>2</sub>O<sub>3</sub> for Ln<sup>3+</sup> lasants we used a home-made Xe-flashlamp-pumped picosecond (≈ 100 ps) Nd<sup>3+</sup>:Y<sub>3</sub>Al<sub>5</sub>O<sub>12</sub> laser emitted at a fundamental wavelength  $\lambda_f = 1.06415 \mu\text{m}$  ( $^4F_{3/2} \rightarrow ^4I_{11/2}$  generation channel of Nd<sup>3+</sup> activator ions). The nearly Gaussian profile of its beam was focused into about 15-mm long ceramic samples with a lens ( $f = 25 \text{ cm}$ ), resulting in beam-waist diameter of about  $160 \mu\text{m}$ . The spectral composition of the SRS and Raman-induced multi-wave mixing was analyzed with a grating monochromator (McPherson Model 270 in Cherny-Turned arrangement) combined with spectrometric system (CSMA) equipped with two Hamamatsu linear image sensors Si-CCD (3923-1024Q) and CCD-InGaAs (G9204-512D) offering good enough spectral sensitivity from UV till ≈ 1.7  $\mu\text{m}$  (see Fig. 1). In consequence of more careful matching of an excitation scheme and new IR detector compared to our earlier SRS-measurements [8,13] we significant widened Stokes and anti-Stokes wings for

Nonlinear generation		
Wavelength, $\mu\text{m}^a)$	Line $^b)$	Lasing component attribution
Sc <sub>2</sub> O <sub>3</sub> , $\omega_{SRS} \approx 419 \text{ cm}^{-1}$ (see Fig. 2)		
0.3344	ASt <sub>2</sub> $\lambda_{THG}$	$3\omega_f + 2\omega_{SRS}$
0.3495	ASt <sub>1</sub> $\lambda_{THG}$	$3\omega_f + \omega_{SRS}$
0.3547	$\lambda_{THG}$	$3\omega_f$
0.3600	St <sub>1</sub> $\lambda_{THG}$	$3\omega_f - \omega_{SRS}^c)$
0.3656	St <sub>2</sub> $\lambda_{THG}$	$3\omega_f - 2\omega_{SRS}^c)$
0.3712	St <sub>3</sub> $\lambda_{THG}$	$3\omega_f - 3\omega_{SRS}^c)$
0.3771	St <sub>4</sub> $\lambda_{THG}$	$3\omega_f - 4\omega_{SRS}^c)$
0.3832	St <sub>5</sub> $\lambda_{THG}$	$3\omega_f - 5\omega_{SRS}^c)$
0.3894	St <sub>6</sub> $\lambda_{THG}$	$3\omega_f - 6\omega_{SRS}^c)$
0.53207	$\lambda_{SHG}$	$2\omega_f$
0.5761	ASt <sub>19</sub>	$\omega_f - 2\omega_{SRS}$
0.5903	ASt <sub>18</sub>	$\omega_f - 3\omega_{SRS}$
0.6053	ASt <sub>17</sub>	$\omega_f - 4\omega_{SRS}$
0.6211	ASt <sub>16</sub>	$\omega_f - 5\omega_{SRS}$
0.6377	ASt <sub>15</sub>	$\omega_f + 15\omega_{SRS}$
0.6552	ASt <sub>14</sub>	$\omega_f + 14\omega_{SRS}$
0.6737	ASt <sub>13</sub>	$\omega_f + 13\omega_{SRS}$
0.6932	ASt <sub>12</sub>	$\omega_f + 12\omega_{SRS}$
0.7140	ASt <sub>11</sub>	$\omega_f + 11\omega_{SRS}$
0.7360	ASt <sub>10</sub>	$\omega_f + 10\omega_{SRS}$
0.7594	ASt <sub>9</sub>	$\omega_f + 9\omega_{SRS}$
0.7844	ASt <sub>8</sub>	$\omega_f + 8\omega_{SRS}$
0.8110	ASt <sub>7</sub>	$\omega_f + 7\omega_{SRS}$
0.8396	ASt <sub>6</sub>	$\omega_f + 6\omega_{SRS}$
0.8702	ASt <sub>5</sub>	$\omega_f + 5\omega_{SRS}$
0.9031	ASt <sub>4</sub>	$\omega_f + 4\omega_{SRS}$
0.9386	ASt <sub>3</sub>	$\omega_f + 3\omega_{SRS}$
0.9770	ASt <sub>2</sub>	$\omega_f + 2\omega_{SRS}$
1.0187	ASt <sub>1</sub>	$\omega_f + \omega_{SRS}$
1.06415	$\lambda_f$	$\omega_f$
1.1138	St <sub>1</sub>	$\omega_f - \omega_{SRS}$
1.1684	St <sub>2</sub>	$\omega_f - 2\omega_{SRS}$
1.2285	St <sub>3</sub>	$\omega_f - 3\omega_{SRS}$
1.2952	St <sub>4</sub>	$\omega_f - 4\omega_{SRS}$
1.3695	St <sub>5</sub>	$\omega_f - 5\omega_{SRS}$
1.4528	St <sub>6</sub>	$\omega_f - 6\omega_{SRS}$
Lu <sub>2</sub> O <sub>3</sub> , $\omega_{SRS} \approx 392 \text{ cm}^{-1}$ (see Fig. 3)		
0.3498	ASt <sub>1</sub> $\lambda_{THG}$	$3\omega_f + \omega_{SRS}$
0.3547	$\lambda_{THG}$	$3\omega_f$
0.3597	St <sub>1</sub> $\lambda_{THG}$	$3\omega_f - \omega_{SRS}^c)$
0.3648	St <sub>2</sub> $\lambda_{THG}$	$3\omega_f - 2\omega_{SRS}^c)$
0.3701	St <sub>3</sub> $\lambda_{THG}$	$3\omega_f - 3\omega_{SRS}^c)$
0.3756	St <sub>4</sub> $\lambda_{THG}$	$3\omega_f - 4\omega_{SRS}^c)$
0.53207	$\lambda_{SHG}$	$2\omega_f$
0.6382	ASt <sub>16</sub>	$\omega_f + 16\omega_{SRS}$
0.6546	ASt <sub>15</sub>	$\omega_f + 15\omega_{SRS}$

Nonlinear generation		
Wavelength, $\mu\text{m}^a)$	Line $^b)$	Lasing component attribution
0.6718	ASt <sub>14</sub>	$\omega_f + 14\omega_{SRS}$
0.6900	ASt <sub>13</sub>	$\omega_f + 13\omega_{SRS}$
0.7092	ASt <sub>12</sub>	$\omega_f + 12\omega_{SRS}$
0.7294	ASt <sub>11</sub>	$\omega_f + 11\omega_{SRS}$
0.7509	ASt <sub>10</sub>	$\omega_f + 10\omega_{SRS}$
0.7737	ASt <sub>9</sub>	$\omega_f + 9\omega_{SRS}$
0.7979	ASt <sub>8</sub>	$\omega_f + 8\omega_{SRS}$
0.8236	ASt <sub>7</sub>	$\omega_f + 7\omega_{SRS}$
0.8511	ASt <sub>6</sub>	$\omega_f + 6\omega_{SRS}$
0.8805	ASt <sub>5</sub>	$\omega_f + 5\omega_{SRS}$
0.9120	ASt <sub>4</sub>	$\omega_f + 4\omega_{SRS}$
0.9458	ASt <sub>3</sub>	$\omega_f + 3\omega_{SRS}$
0.9822	ASt <sub>2</sub>	$\omega_f + 2\omega_{SRS}$
1.0215	ASt <sub>1</sub>	$\omega_f + \omega_{SRS}$
1.06415	$\lambda_f$	$\omega_f$
1.1105	St <sub>1</sub>	$\omega_f - \omega_{SRS}$
1.1610	St <sub>2</sub>	$\omega_f - 2\omega_{SRS}$
1.2114	St <sub>3</sub>	$\omega_f - 3\omega_{SRS}$
1.2773	St <sub>4</sub>	$\omega_f - 4\omega_{SRS}$
1.3446	St <sub>5</sub>	$\omega_f - 5\omega_{SRS}$

<sup>a)</sup> Measurement accuracy is 0.0003  $\mu\text{m}$ .

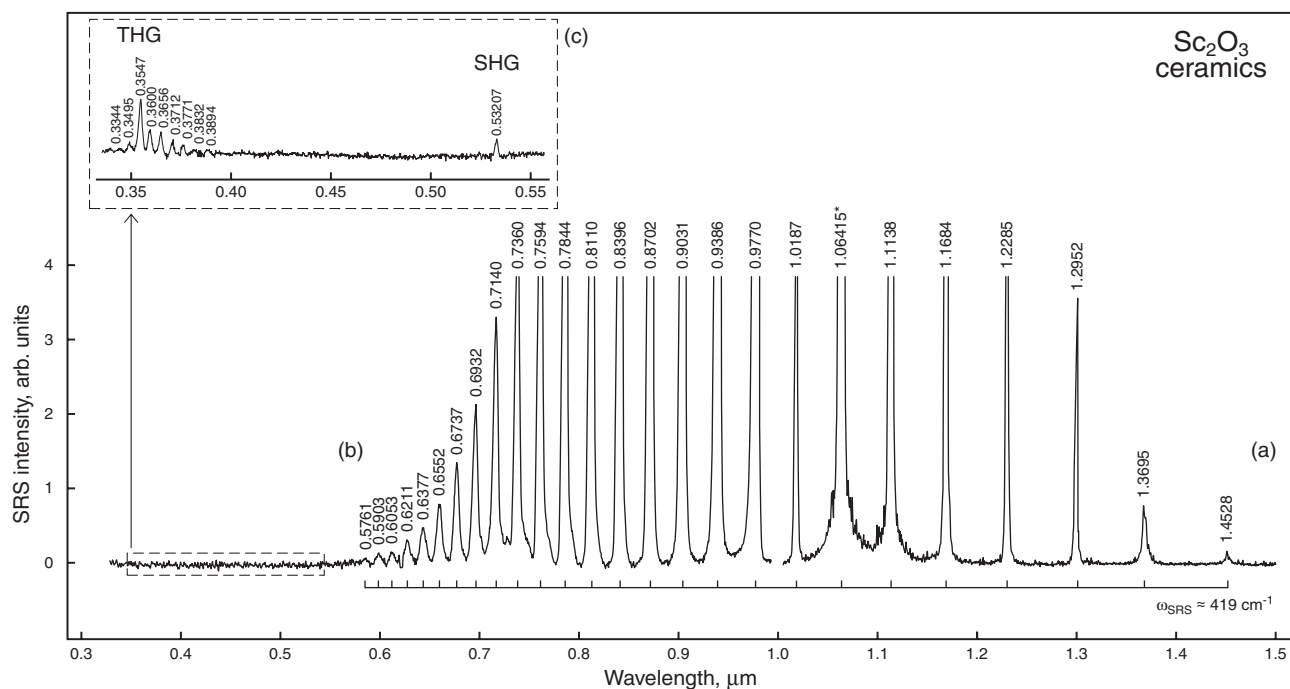
<sup>b)</sup> For example, the condition notation of cascaded generation ASt<sub>1</sub> $\lambda_{THG}$  is defined as the first anti-Stokes component connected with THG of fundamental pump emission.

<sup>c)</sup> One of possible five-wave parametric interaction involving pump and Stokes lasing emission.

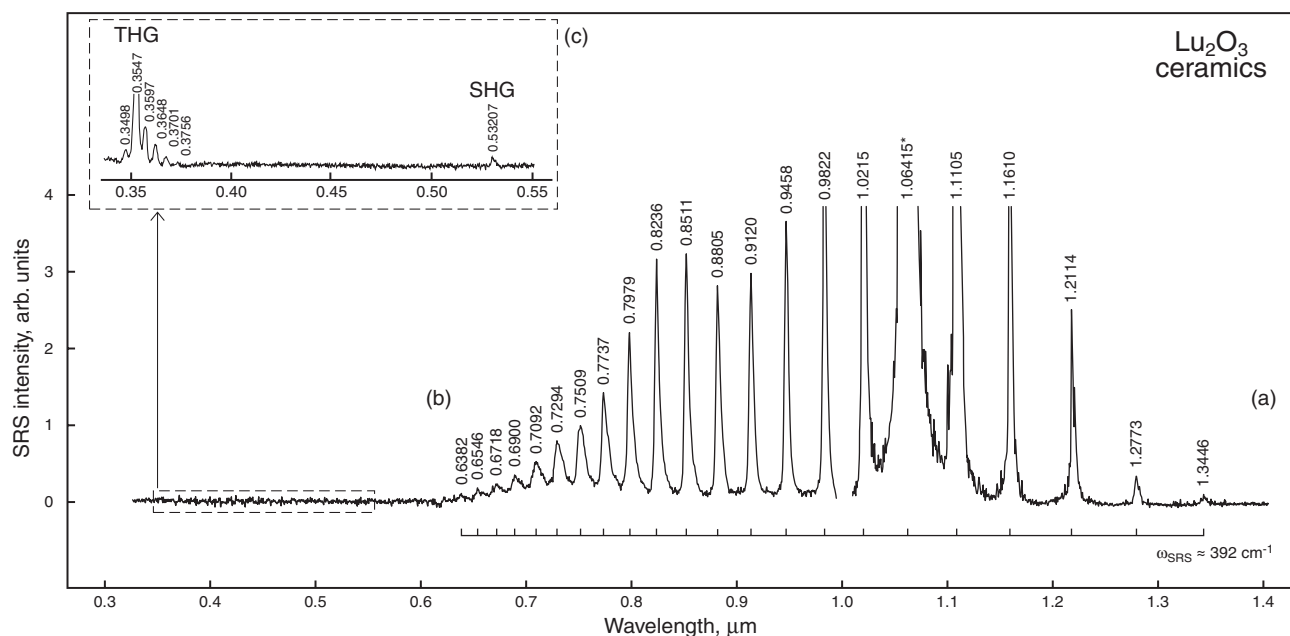
**Table 2** Room-temperature spectral composition of nonlinear-laser generation in crystalline ceramics based on cubic oxides Sc<sub>2</sub>O<sub>3</sub> and Lu<sub>2</sub>O<sub>3</sub> under picosecond Nd<sup>3+</sup>:Y<sub>3</sub>Al<sub>5</sub>O<sub>12</sub>-laser excitation at its fundamental wavelength  $\lambda_f = 1.06415 \mu\text{m}$

both studied ceramics, from 0.5761  $\mu\text{m}$  to 1.4528  $\mu\text{m}$  for Sc<sub>2</sub>O<sub>3</sub> and from 0.6382  $\mu\text{m}$  to 1.3446  $\mu\text{m}$  wavelengths for Lu<sub>2</sub>O<sub>3</sub>. These results are shown in Figs. 2a,b and Figs. 3a,b and listed in Table 2.

In an effort to investigate of our second problem in Sc<sub>2</sub>O<sub>3</sub> and Lu<sub>2</sub>O<sub>3</sub> ceramics connected with exacting supervision their possible SHG, THG, and  $\chi^{(3)}$ -nonlinear multi-wave parametric lasing using filters and other standard experimental contrivances. By this we significant decreased unwanted (saturated) influence of strong one-micron pump radiation and intensive Stokes and anti-Stokes bands emission on the Si-CCD sensor and thus significantly enhanced its sensitivity in the visible and UV spectral regions. The results of these measurements are shown in Fig. 2c and Fig. 3c. As seen, in both ceramics under picosecond one-micron pumping we recorded relatively low-intensity signals of SHG at  $\lambda_{SHG} = 0.53207 \mu\text{m}$  and THG at  $\lambda_{THG} = 0.3547 \mu\text{m}$  wavelengths, as well as in the neighbourhood of latter several cascaded five-wave mix-



**Figure 2** Room-temperature spectra of nonlinear self-frequency lasing in fine-grained  $\text{Sc}_2\text{O}_3$  ceramics obtained with excitation of one-micron generation of picosecond  $\text{Nd}^{3+}:\text{Y}_3\text{Al}_5\text{O}_{12}$ -laser recorded: (a) and (b) with InGaAs-CCD and Si-CCD sensors, respectively; (c) with Si-CCD sensor and under strong attenuation of pump and its intensive Stokes and anti-Stokes signals (see inset). The wavelength of all lasing lines given in  $\mu\text{m}$  (pump line is marked by an asterisk). Stokes and anti-Stokes lines (see spectra (a) and (b)) related to SRS-promoting vibration modes  $\omega_{\text{SRS}} \approx 419 \text{ cm}^{-1}$  are indicated by horizontal scale brackets



**Figure 3** Room-temperature spectra of nonlinear self-frequency lasing in fine-grained  $\text{Lu}_2\text{O}_3$  ceramics obtained with excitation of one-micron generation of picosecond  $\text{Nd}^{3+}:\text{Y}_3\text{Al}_5\text{O}_{12}$ -laser recorded: (a) and (b) with InGaAs-CCD and Si-CCD sensors, respectively; (c) with Si-CCD sensor and under strong attenuation of pump and its intensive Stokes and anti-Stokes signals (see inset). Stokes and anti-Stokes lines (see spectra (a) and (b)) related to SRS-promoting vibration modes  $\omega_{\text{SRS}} \approx 392 \text{ cm}^{-1}$  are indicated by horizontal scale brackets. Other notation as in Fig. 2

ing UV components. Whereas all observed  $\chi^{(3)}$ -nonlinear components in  $\text{Sc}_2\text{O}_3$  and  $\text{Lu}_2\text{O}_3$  ceramics are sufficiently understandable and in a great part agrees with the data on measurements of nonlinear refractive indices  $n_2$  (which directly related to  $\chi^{(3)}$ -susceptibility) [15], as well as with recently achieved efficient sub-100 fs Kerr-lens mode-locked lasing in  $\text{Yb}^{3+}:\text{Sc}_2\text{O}_3$  ceramics [4], while the expected and observed SHG need be investigated with great care. The case is that the efficiency of recorded self-frequency doubling was very low in both ceramics studied. It should be noted here, that weak SHG could be associated also with induced  $\chi^{(2)}$ -nonlinearity (local mechanical stress) and with arising plasma in micro-interstices (bubbles or pores) in centrosymmetric crystalline materials under focusing strong laser excitation. But, these possible reasons are not likely to take place in our case.

### 3. Conclusion

We have discovered several new nonlinear-laser effects in highly transparent crystalline host-ceramics (for  $\text{Ln}^{3+}$  lasants) based on cubic oxides  $\text{Sc}_2\text{O}_3$  and  $\text{Lu}_2\text{O}_3$ , namely: the non-phase-matched THG and nonlinear cascaded  $\chi^{(3)} \leftrightarrow \chi^{(3)}$  lasing in UV spectral area arising from one-micron picosecond laser excitation and Raman induced Stokes and anti-Stokes lasing fields in near-IR, as well as SHG arising from induced  $\chi^{(2)}$ -nonlinearity related to fundamental property of fine-grained nature of ceramics studied. It is worth noting that nonlinear laser cascading in crystalline materials has been observed up to now only of the  $\chi^{(2)} \leftrightarrow \chi^{(3)}$  type (see, e.g. [16-18]). Thanks to the improvement of the excitation and recorded condition we also significantly widened of SRS and Raman induced four wave mixing lasing wings. So, we recorded 25 Stokes and anti-Stokes lasing sidebands covered spectral region from  $0.5761 \mu\text{m}$  to  $1.4528 \mu\text{m}$  for  $\text{Sc}_2\text{O}_3$  and 21 lines within  $0.6382 \mu\text{m}$  and  $1.3446 \mu\text{m}$  wavelengths for  $\text{Lu}_2\text{O}_3$  ceramics.

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