

**Abstract:** High-order stimulated Raman scattering (SRS) and cascaded  $\chi^{(3)} \rightarrow \chi^{(2)}$  generation effects in new nonlinear-laser crystals of  $\text{PbB}_4\text{O}_7$  were observed with picosecond laser pumping. All registered  $\chi^{(3)}$ - and  $\chi^{(2)}$ -lasing components in the visible and near-IR were identified and attributed to the SRS-promoting mode  $\omega_{\text{SRS}} \approx 148 \text{ cm}^{-1}$  of the studied crystal.



Example of a grown crystal of  $\text{PbB}_4\text{O}_7$ , together with two crystal samples that were cut from the bulk of the crystal

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# High-order stimulated Raman scattering and cascaded nonlinear lasing effects in crystals of $(\chi^{(3)} \rightarrow \chi^{(2)})$ -active orthorhombic $\text{PbB}_4\text{O}_7$

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**Key words:** stimulated Raman scattering; Raman borate crystal;  $\text{PbB}_4\text{O}_7$ ; lead tetraborate; nonlinear laser cascading; Stokes and anti-Stokes generation; Raman laser converters

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## 1. Introduction

Borate crystals nowadays are a well-established family of active materials for laser frequency doublers and stimulated Raman scattering (SRS) frequency converters, that base either on  $\chi^{(2)}$  and  $\chi^{(3)}$  nonlinearities or cascaded  $\chi^{(3)} \leftrightarrow \chi^{(2)}$  processes, as well as for solid-state lasers, that can generate stimulated emission (SE) of their trivalent lanthanide ( $\text{Ln}^{3+}$ ) activators (see Table 1 and [1,2]). Among them the nonlinear-laser crystal  $\text{PbB}_4\text{O}_7$  is a member of the isomorphic series of polar orthorhombic tetraborates  $M^{II}\text{B}_4\text{O}_7$  (with  $M^{II} = \text{Pb}$  [3], Sr [4], Eu [5],

Ca (high pressure) [6], Hg (high pressure) [7], and Sn (high-pressure) [8]) and had been subject to investigations of nonlinear optical properties already in the eighties. With its electro-optic constants  $\text{PbB}_4\text{O}_7$  ranges among the known borates with highest value of this property [9].

Recently, lead tetraborate was found to possess the highest value of tensor coefficients of second harmonic generation (SHG)  $d_{ijk}^{\text{SHG}}$  among all non-centrosymmetric borates investigated so far [10]. Unfortunately, as it was already stated also by [11], the refractive indices of  $\text{PbB}_4\text{O}_7$  do not allow the realization of phase matching conditions for second harmonic generation (SHG). In this letter, we

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Crystal	Space group	SE <sup>a)</sup>	SHG	THG <sup>b)</sup>	SRS	Self-FG (SE) <sup>c)</sup>	Self-FD (SRS) <sup>d)</sup>	Self-SRS (SE) <sup>e)</sup>	Self-SRS (SHG) <sup>f)</sup>	Self-SFM <sup>g)</sup>	Self-DFH <sup>h)</sup>	OPO <sup>i)</sup>
<b>Monoclinic crystals</b>												
Ca <sub>4</sub> Y(BO <sub>3</sub> ) <sub>3</sub> O	C <sub>s</sub> <sup>3</sup>	+	+		+	+		+				
Ca <sub>4</sub> Gd(BO <sub>3</sub> ) <sub>3</sub> O	C <sub>s</sub> <sup>3</sup>	+	+		+							
Sr <sub>4</sub> Y(BO <sub>3</sub> ) <sub>3</sub> O	C <sub>s</sub> <sup>3</sup>	+										
La <sub>2</sub> CaB <sub>10</sub> O <sub>19</sub>	C <sub>2</sub> <sup>3</sup>	+	+			+						
BiB <sub>3</sub> O <sub>6</sub>	C <sub>2</sub> <sup>3</sup>	<sup>j)</sup>	+	+(?)	+	+(?)			+	+		+
<b>Orthorhombic crystals</b>												
LiB <sub>3</sub> O <sub>5</sub>	C <sub>2v</sub> <sup>9</sup>		+									
K <sub>3</sub> Nb <sub>3</sub> O <sub>6</sub> (BO <sub>3</sub> ) <sub>2</sub>	C <sub>2v</sub> <sup>2</sup>		+		+							
CsB <sub>3</sub> O <sub>5</sub>	D <sub>2</sub> <sup>4</sup>		+	+(?)								
PbB <sub>4</sub> O <sub>7</sub>	C <sub>2v</sub> <sup>7</sup>		+ <sup>k)</sup>		+					+		
<b>Tetragonal crystals</b>												
Li <sub>2</sub> B <sub>4</sub> O <sub>7</sub>	C <sub>4v</sub> <sup>12</sup>		+ <sup>l,m)</sup>	+ <sup>l)</sup>	+		+		+	+		
LiGeBO <sub>4</sub>	S <sub>4</sub> <sup>2</sup>				+		+ <sup>k)</sup>					
CsLiB <sub>6</sub> O <sub>10</sub>	D <sub>2d</sub> <sup>12</sup>		+									
<b>Trigonal crystals</b>												
β-YAl <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>	D <sub>3</sub> <sup>7</sup>	+	+			+						
β-BaB <sub>2</sub> O <sub>4</sub>	C <sub>3v</sub> <sup>6</sup>	<sup>j)</sup>	+ <sup>m)</sup>	+	+				+	+ <sup>n)</sup>		+
β-LaBGeO <sub>5</sub>	C <sub>3</sub> <sup>2</sup>	+	+ <sup>o)</sup>		+	+	+	+	+	+	+	
β-LaSc <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>	D <sub>3</sub> <sup>7</sup>	+	+			+						
β-CeSc <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>	D <sub>3</sub> <sup>7</sup>	+	+			+						
β-GdAl <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>	D <sub>3</sub> <sup>7</sup>	+	+			+				+		
<b>Hexagonal crystal</b>												
BaCaBO <sub>3</sub> F	D <sub>3h</sub> <sup>3</sup>	+	+(?)									

a) Presently, in these boron containing non-centrosymmetric crystals SE was obtained with four Ln<sup>3+</sup> lasants: Pr<sup>3+</sup>, Nd<sup>3+</sup>, Er<sup>3+</sup>, and Yb<sup>3+</sup>.

b) THG: third harmonic generation.

c) Self-FD(SE): self-frequency doubling, i.e., cascaded SHG from arising SE in Ln<sup>3+</sup>-ion doped crystals with non-laser and laser pumping.

d) Self-FD(SRS): self-frequency doubling, i.e., cascaded SHG from arising Stokes and anti-Stokes generation in undoped crystals with external laser excitation.

e) Self-SRS(SE): self-stimulated Raman scattering, i.e., cascaded laser Raman Stokes and anti-Stokes generation by the action of arising SE in Ln<sup>3+</sup>-ion doped crystals with external laser radiation.

f) Self-SRS(SHG): self-stimulated Raman scattering, i.e., cascaded laser Raman Stokes and anti-Stokes generation by the action of arising SHG in undoped crystals with external laser radiation.

g) Self-SFM: self-sum-frequency mixing, i.e., cascaded summing parametric generation (up-conversion processes) between arising secondary laser emissions (e.g., SE, SRS, SHG, and others), as well as laser excitation radiation in Ln<sup>3+</sup>-ion doped and undoped crystals with external non-laser and laser pumping.

h) Self-DFG: self-difference-frequency generation, i.e., cascaded difference parametric interaction (down-conversion processes) between arising secondary laser emissions and laser pumping radiation.

i) OPO: optical parametric oscillation.

j) Can be activated by Ln<sup>3+</sup> lasants.

k) Non phase-matchable frequency doubling in the visible.

l) Cherenkov-type SHG and THG were observed as well.

m) It is possible also the collinear fourth harmonic generation with birefringent phase-matching.

n) Also, self-sum-frequency generation in an optical parametric amplifier by mixing between the pumping and arising idler wavelengths.

o) Cherenkov-type SHG was observed as well.

**Table 1** Selected laser and non-centrosymmetric nonlinear-laser borate crystals and their  $\chi^{(2)}$ -,  $\chi^{(3)}$ -, and cascaded ( $\chi^{(3)} \leftrightarrow \chi^{(2)}$ )-frequency conversion and lasing effects

report on the first observation of high-order Raman Stokes and anti-Stokes generation and cascaded ( $\chi^{(3)} \rightarrow \chi^{(2)}$ )-lasing effects in PbB<sub>4</sub>O<sub>7</sub> single crystals with picosecond one-micron laser excitation.

## 2. Crystallography

The crystal structure of PbB<sub>4</sub>O<sub>7</sub> (that was already mentioned to be isomorphous to SrB<sub>4</sub>O<sub>7</sub> by [3]) was first de-

termined by [11]. A detailed structure investigation with an emphasis on the influence of the stereochemical active lone electron pair of Pb<sup>2+</sup> was recently presented by [12]. PbB<sub>4</sub>O<sub>7</sub> crystallizes in the non-centrosymmetric, polar space group *Pnm*2<sub>1</sub> with  $a_1 = 4.4535(4)$  Å,  $a_2 = 10.8346(9)$  Å, and  $a_3 = 4.2441(3)$  Å [12] (see also footnote <sup>b)</sup> in Table 2). The crystal structure consists of exclusively four-fold (tetrahedrally) coordinated boron atoms and lead atoms with an irregular oxygen coordination of which the coordination number is not clearly defined. Setting a cut-

Characteristic																																	
Space group [3]	$C_{2v}^7 - Pnm2_1$ (No. 31) <sup>b)</sup>																																
Unit cell parameters, Å [12]	$a_1 = 4.4535(4)$ (= a); $a_2 = 10.8346(9)$ (= b); $a_3 = 4.2441(3)$ (= c)																																
Formula units per unit cell [3]	$Z = 2$																																
Fractional coordinates, site symmetry (ss) and coordination number (CN) of atoms [12]	<table border="1"> <thead> <tr> <th><i>x</i></th> <th><i>y</i></th> <th><i>z</i></th> <th>ss</th> </tr> </thead> <tbody> <tr> <td>Pb: 0.69835(1) CN = 10<sup>c)</sup></td> <td>0</td> <td>0</td> <td><math>m(C_s)</math></td> </tr> <tr> <td>B1: 0.8258(2) CN = 4</td> <td>0.3779(1)</td> <td>0.0067(9)</td> <td><math>1(C_1)</math></td> </tr> <tr> <td>B2: 0.3230(3) CN = 4</td> <td>0.2483(1)</td> <td>0.0345(5)</td> <td><math>1(C_1)</math></td> </tr> <tr> <td>O1: 0.2657(3)</td> <td>0</td> <td>0.6140(4)</td> <td><math>m(C_s)</math></td> </tr> <tr> <td>O2: 0.1400(2)</td> <td>0.3561(1)</td> <td>0.0822(3)</td> <td><math>1(C_1)</math></td> </tr> <tr> <td>O3: 0.7701(2)</td> <td>0.3637(1)</td> <td>0.6745(3)</td> <td><math>1(C_1)</math></td> </tr> <tr> <td>O4: 0.3709(2)</td> <td>0.2200(1)</td> <td>0.6799(2)</td> <td><math>1(C_1)</math></td> </tr> </tbody> </table>	<i>x</i>	<i>y</i>	<i>z</i>	ss	Pb: 0.69835(1) CN = 10 <sup>c)</sup>	0	0	$m(C_s)$	B1: 0.8258(2) CN = 4	0.3779(1)	0.0067(9)	$1(C_1)$	B2: 0.3230(3) CN = 4	0.2483(1)	0.0345(5)	$1(C_1)$	O1: 0.2657(3)	0	0.6140(4)	$m(C_s)$	O2: 0.1400(2)	0.3561(1)	0.0822(3)	$1(C_1)$	O3: 0.7701(2)	0.3637(1)	0.6745(3)	$1(C_1)$	O4: 0.3709(2)	0.2200(1)	0.6799(2)	$1(C_1)$
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Density, g cm <sup>-3</sup> [11, 12]	$d_x \approx 5.88$																																
Melting temperature, K [13]	$T_m \approx 1047$																																
Method of crystal growth	top-seeding technique [14, 15], modified Czochralski [15–17]																																
Linear optical character	biaxial negative ( $n_1^0 \gtrsim n_3^0 > n_2^0$ )																																
Optical transparency range, μm <sup>d)</sup>	$\approx 0.23 - \approx 3.2$ (see also Fig. 3)																																
Refractive index (modified Sellmeier equation) [10] <sup>e)</sup>	$n^2(\lambda) = D_1 + \frac{D_2}{(\lambda^2 - D_3)} - D_4\lambda^2$ (see also Fig. 3)																																
Nonlinearity	$\chi^{(2)}$ and $\chi^{(3)}$																																
Nonlinear optical susceptibilities, 10 <sup>-12</sup> m V <sup>-1</sup> [10] <sup>f)</sup>	$d_{311}^{SHG} = 2.3(3)$ ; $d_{322}^{SHG} = 2.8(5)$ ; $d_{333}^{SHG} = 4.0(4)$ ; $d_{113}^{SHG} = 0.68(5)$ ; $d_{223}^{SHG} = 0.57(5)$																																
Phase matching condition for SHG	not phase-matchable in the entire transparency range																																
Linear electro-optic coefficients at constant stress, 10 <sup>-12</sup> m V <sup>-1</sup> [9] <sup>g)</sup>	$r_{113}^\sigma = 2.35(8)$ ; $r_{223}^\sigma = 2.40(8)$ ; $r_{333}^\sigma = 2.83(9)$ ; $r_{131}^\sigma = 0.68(5)$ ; $r_{232}^\sigma = 0.95(7)$																																
Piezoelectric (linear electrostrictive) coefficients, 10 <sup>-12</sup> m V <sup>-1</sup> [9] <sup>h)</sup>	$d_{311} = 2.8(2)$ ; $d_{322} = 2.6(2)$ ; $d_{333} = \pm 0.0(1)$ ; $d_{113} = 2.1(1)$ ; $d_{223} = 1.7(2)$																																
Pyroelectric coefficient at constant stress and its temperature dependence, <sup>i)</sup> 10 <sup>-6</sup> C m <sup>-2</sup> K <sup>-1</sup> [18]	$p_3^\sigma(T) = 19.81 - 2.741 \times 10^{-2}T + 2.924 \times 10^{-5}T^2$ (standard deviation: 0.4)																																
Phonon spectrum extension, cm <sup>-1</sup> <sup>j)</sup>	$\approx 1100$																																
Energy of SRS-promoting vibration mode, cm <sup>-1</sup>	$\omega_{SRS} \approx 148$ (see also Fig. 4)																																
Width of Raman shifted line related to SRS-promoting vibration transition, cm <sup>-1</sup>	$\Delta\nu_R \approx 6$ cm <sup>-1</sup> (see also Fig. 5a)																																
Possible applications	UV/VIS electro-optic Q-switchers/modulators, surface acoustic wave devices [15], Raman laser converters																																

<sup>a)</sup> Limit of probable error in parentheses.

<sup>b)</sup> Original data from [12] that are given in standard setting  $Pnm2_1$  were transformed to the non-standard setting  $Pnm2_1$ , that had already been used for all previous physical investigations. Note that in [3] and [11] a non-standard setting  $P2_1nm$  is used.

<sup>c)</sup> Using a cut-off value for the nearest neighbours of 3.1 Å.

<sup>d)</sup> For  $\approx 1.7$ -mm thick (100)-plate.

<sup>e)</sup> Sellmeier coefficients:  $\lambda$  is in μm, (the refractive indices were determined in the wavelength range 0.365 – 1.083 μm using the prism method and corrected with the refractive index of air;  $\xi^2$  is the sum of the squares of the residuals). See also [16, 17].

	$D_1$	$D_2$	$D_3$	$D_4$	$\xi^2$
$n_1^0$	3.644911	0.036662	0.0272	0.022440	$0.1 \times 10^{-8}$
$n_2^0$	3.625194	0.035386	0.0265	0.024742	$0.5 \times 10^{-8}$
$n_3^0$	3.638438	0.036738	0.0271	0.021697	$4.8 \times 10^{-8}$

<sup>f)</sup> For  $\lambda = 1.064$  μm wavelength.

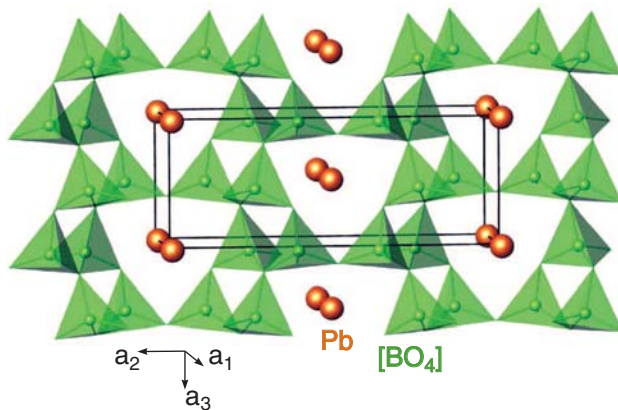
<sup>g)</sup> For  $\lambda = 0.6328$  μm wavelength.

<sup>h)</sup> Further published data of piezoelectric constants (as well as elastic and dielectric constants) by [19] were not included due to inconsistencies and severe confusions in these publications.

<sup>i)</sup> Within temperature range 163 – 400 K.

<sup>j)</sup> From spontaneous Raman scattering spectra.

**Table 2** Crystallographic and some physical properties of orthorhombic  $PbB_4O_7$  single crystals at room temperature (unless indicated otherwise)<sup>a)</sup>



**Figure 1** (online color at [www.lphys.org](http://www.lphys.org)) Plot of the crystal structure of  $\text{PbB}_4\text{O}_7$ .  $[\text{BO}_4]$  groups are marked with green tetrahedra, Pb is marked with large orange spheres. Pb atoms are located in tubular voids of the borate network that run along  $a_1$  and  $a_3$ . (Data taken from [12])



**Figure 2** (online color at [www.lphys.org](http://www.lphys.org)) Example of a grown crystal of  $\text{PbB}_4\text{O}_7$ , together with two crystal samples that were cut from the bulk of the crystal

off value for the nearest neighbour distances at 3.1 Å lead is 10-fold coordinated with oxygen (the distance between Pb and the next nearest cation, boron, is 3.17 Å). The  $[\text{BO}_4]$  borate units are linked via common oxygen atoms to a three-dimensional network with tubular voids, where the lead atoms are situated, that run parallel to the  $a_1$  and the  $a_3$  axis of the structure, see Fig. 1. Lead as well as one of the oxygen atoms (O1) are in a special position

Stokes and anti-Stokes lasing components		
Wavelength, $\mu\text{m}$ <sup>a)</sup>	Line	SRS- and RFWM-line attribution <sup>b)</sup>
0.5279	SFM	$\omega_f + \omega_{\text{AS}t1}(\omega_f + \omega_{\text{SRS}})$
0.53207	SHG( $\lambda_f/2$ )	$2\omega_f$
0.5363	SFM	$\omega_f + \omega_{\text{St}1}(\omega_f - \omega_{\text{SRS}})$
0.5406	SFM	$\omega_f + \omega_{\text{St}2}(\omega_f - 2\omega_{\text{SRS}})$
0.5450	SFM	$\omega_f + \omega_{\text{St}3}(\omega_f - 3\omega_{\text{SRS}})$
0.8719	AS $t_{14}$	$\omega_f + 14\omega_{\text{SRS}}$
0.8833	AS $t_{13}$	$\omega_f + 13\omega_{\text{SRS}}$
0.8950	AS $t_{12}$	$\omega_f + 12\omega_{\text{SRS}}$
0.9070	AS $t_{11}$	$\omega_f + 11\omega_{\text{SRS}}$
0.9194	AS $t_{10}$	$\omega_f + 10\omega_{\text{SRS}}$
0.9320	AS $t_9$	$\omega_f + 9\omega_{\text{SRS}}$
0.9451	AS $t_8$	$\omega_f + 8\omega_{\text{SRS}}$
0.9585	AS $t_7$	$\omega_f + 7\omega_{\text{SRS}}$
0.9723	AS $t_6$	$\omega_f + 6\omega_{\text{SRS}}$
0.9865	AS $t_5$	$\omega_f + 5\omega_{\text{SRS}}$
1.0011	AS $t_4$	$\omega_f + 4\omega_{\text{SRS}}$
1.0162	AS $t_3$	$\omega_f + 3\omega_{\text{SRS}}$
1.0317	AS $t_2$	$\omega_f + 2\omega_{\text{SRS}}$
1.0477	AS $t_1$	$\omega_f + \omega_{\text{SRS}}$
1.06415	$\lambda_f$	$\omega_f$
1.0812	St $_1$	$\omega_f - \omega_{\text{SRS}}$
1.0988	St $_2$	$\omega_f - 2\omega_{\text{SRS}}$
1.1169	St $_3$	$\omega_f - 3\omega_{\text{SRS}}$
1.1357	St $_4$	$\omega_f - 4\omega_{\text{SRS}}$
1.1551	St $_5$	$\omega_f - 5\omega_{\text{SRS}}$
1.1752	St $_6$	$\omega_f - 6\omega_{\text{SRS}}$

<sup>a)</sup> Measurement accuracy is  $\pm 0.0003 \mu\text{m}$ .

<sup>b)</sup>  $\omega_{\text{SRS}} \approx 148 \text{ cm}^{-1}$ .

**Table 3** Room-temperature spectral composition of Stokes and anti-Stokes generation in orthorhombic  $\text{PbB}_4\text{O}_7$  single crystals with picosecond  $\text{Nd}^{3+}:\text{Y}_3\text{Al}_5\text{O}_{12}$ -laser pumping at  $\lambda_f = 1.06415 \mu\text{m}$  wavelength under excitation geometry  $c(qq)c$  (with  $q \parallel (e_1 + e_2)$ )

with site symmetry  $m$ , all other atoms are in general position with site symmetry 1. Since  $\text{PbB}_4\text{O}_7$  melts congruently [13] in principle single crystals can be grown from a melt of stoichiometric composition. However, due to the rather high viscosity of the melt a slight excess of  $\text{PbO}$ , that reduces the viscosity to some extent, proved to be advantageous. The crystals used in our study were grown in our laboratory by the top seeding technique without crystal pulling or rotation, as it has been described already in [14]. The crystals were of high optical quality with dimensions up to  $20 \times 28 \times 55 \text{ mm}^3$ . Fig. 2 gives an example of a grown crystal together with samples cut from the bulk. For the investigation and description of all physical properties a Cartesian reference system  $\{e_i\}$  with  $e_i \parallel a_i$  (“crystalphysical system”) is used. The positive direction of the polar diad  $a_3$ -axis is defined by the positive sign of the transverse piezoelectric coefficient  $d_{311}$  (or  $d_{322}$ ). Our SRS measurements were performed on two crystal samples with different orientations that were cut and prepared



Vibrational mode wave numbers, $\text{cm}^{-1}$		Assignment <sup>b)</sup>
$c(bb)c$ <sup>a)</sup> A <sub>1</sub> –TO (see Fig. 4b)	$c(aa)c$ <sup>a)</sup> A <sub>1</sub> –LO (see Fig. 4a)	
89 w 103 m 121 vw 148 vs	92 vw 105 w 121 w 148 vs	T' (Pb <sup>2+</sup> , B <sup>3+</sup> )
248 s 261 m 273 vw	262 m 273 m	$\delta(\text{BOB})$
293 s 353 vs	293 vw 353 vs	$\delta_s(\text{BO}_4) - \nu_2$
410 w	410 w 420 w 433 vw	$\delta_{as}(\text{BO}_4) - \nu_4 + \text{T}'(\text{B}^{3+})$
485 s	485 s 504 vw	$\nu_s(\text{BOB}) + \text{T}'(\text{B}^{3+})$
527 vw 545 vw 564 w	527 vw 564 s 623 s	$\nu_s(\text{BO}_4) - \nu_1$
841 m	697 m	$\nu_{as}(\text{BOB})$
948 vw 1008 vw 1093 s	907 vw 1007 s 1087 vw	$\nu_{as}(\text{BO}_4) - \nu_4$

<sup>a)</sup> Here: vw – very weak, w – weak, m – medium, s – strong, vs – very strong.

<sup>b)</sup> Here modes: T' – lattice translation,  $\delta$  – bending,  $\delta_s$  – symmetric bending,  $\delta_{as}$  – antisymmetric bending,  $\nu_s$  – symmetric stretching, and  $\nu_{as}$  – asymmetric.

**Table 4** TO and LO vibration Raman A<sub>1</sub>-spectra of the orthorhombic PbB<sub>4</sub>O<sub>7</sub> crystal for two excitation geometries

with polished plane parallel faces. Two samples of orientation  $[100] \times [010] \times [001]$  and  $[100] \times [011]^e \times [0\bar{1}1]^e$ , respectively, were used: sample 1:  $10.26 \times 7.00 \times 6.34 \text{ mm}^3$ ; sample 2:  $12.24 \times 7.58 \times 8.54 \text{ mm}^3$ . Since the relatively small birefringence of PbB<sub>4</sub>O<sub>7</sub> does not allow the realization of phase matching conditions for SHG the study of cascaded  $\chi^{(2)} \leftrightarrow \chi^{(3)}$  processes is limited to non-phase-matched processes. It should be mentioned, however, that PbB<sub>4</sub>O<sub>7</sub> possesses the highest SHG coefficients among the borate family (especially  $d_{333}^{SHG} = 4.0(4) \text{ pm V}^{-1}$  [10]). Some known physical properties of orthorhombic PbB<sub>4</sub>O<sub>7</sub> single crystals are summarized in Table 2.

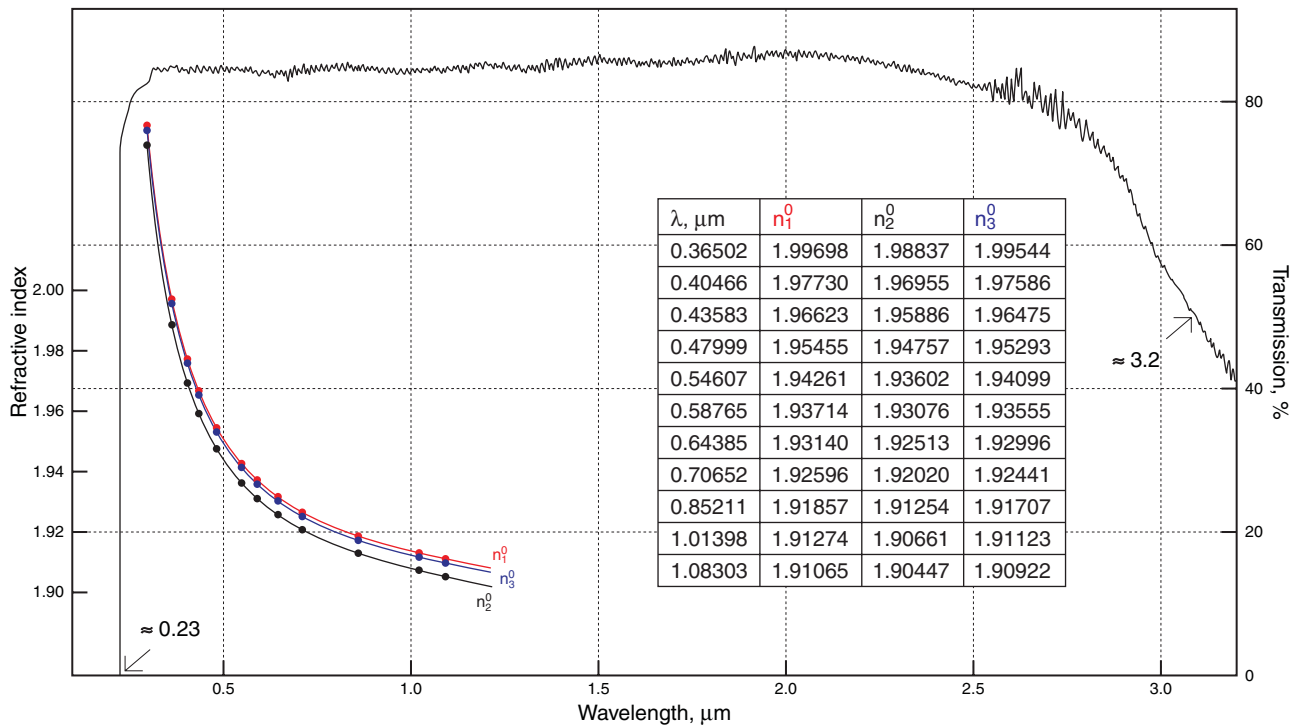
### 3. Stimulated and spontaneous Raman scattering

For the excitation of single-pass lasing Raman Stokes components in oriented orthorhombic non-

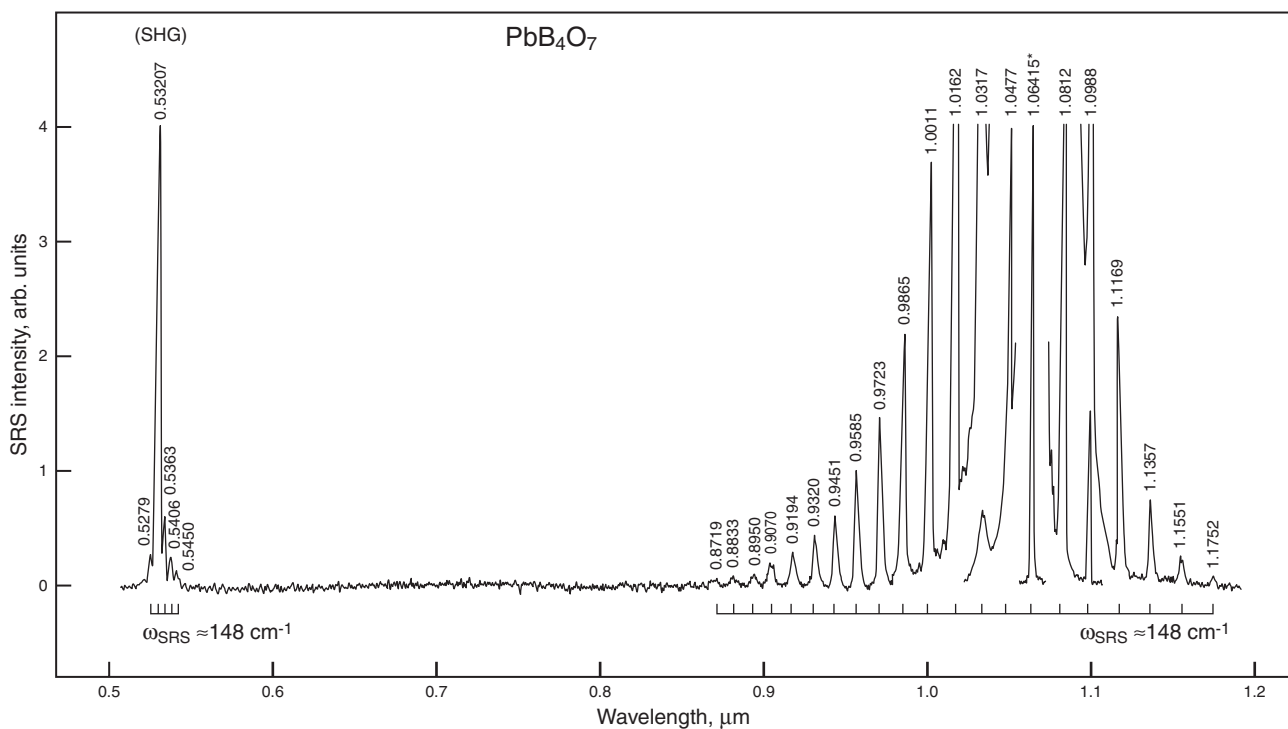
centrosymmetric PbB<sub>4</sub>O<sub>7</sub> single crystals we used a home-made Xe-flashlamp pumped picosecond Nd<sup>3+</sup>:Y<sub>3</sub>Al<sub>5</sub>O<sub>12</sub> mode-locked laser with a two-pass Nd<sup>3+</sup>:Y<sub>3</sub>Al<sub>5</sub>O<sub>12</sub> amplifier that can generate  $\approx 110$  ps pulses at  $\lambda_f = 1.06415 \mu\text{m}$  wavelength ( ${}^4\text{F}_{3/2} \rightarrow {}^4\text{I}_{11/2}$  SE channel) (see, e.g. [2,20]). Its beam with nearly Gaussian profile is focused into the  $(\chi^{(3)} + \chi^{(2)})$  active PbB<sub>4</sub>O<sub>7</sub> samples with a lens ( $f = 250 \text{ mm}$ ), resulting in a beam-waist diameter of about  $160 \mu\text{m}$ . The spectral composition of the nonlinear lasing emission in the visible and near-IR was investigated with a monochromator in Czerny-Turner arrangement (McPherson Model 270 with a grating of 150 lines/mm) and recorded by a spectrometric system with a Si-CCD array sensor (Hamamatsu S3923-1024Q with 1024 pixels). In the SRS experiments that were performed with different excitation orientations and with maximum possible pump power at  $\lambda_f = 1.06415 \mu\text{m}$  wavelength (up to optical damage threshold) for both samples multiple Stokes and anti-Stokes lasing component with equal energy spacing  $\omega_{SRS} \approx 148 \text{ cm}^{-1}$  were observed. Due to  $(\chi^{(3)} + \chi^{(2)})$  nonlinearity of the PbB<sub>4</sub>O<sub>7</sub> crystal in addition to their multiple  $\chi^{(3)}$ -sidebands (which belong to the fundamental one-micron radiation) in the “green” spectral region a group of lines occurs in some pump geometries at proper pump power which are caused by cascaded  $\chi^{(3)} \rightarrow \chi^{(2)}$  processes. These lines result from summing parametric interaction between pump and Stokes/anti-Stokes lasing photons ( $\omega_{SRS} + \omega_{St/Ast}$ ). One of these spectra is shown in Fig. 4. Results of assignment of all recorded lines are listed in Table 3. It should be noted here that the observed SHG signal is not the result of a phase-matched process.

Since all SRS experiments were carried out under the steady-state (ss) pumping conditions  $\tau_p \gg T_2 = (\pi\Delta\nu_R)^{-1} \approx 1.8 \text{ ps}$  (here  $T_2$  is the phonon dephasing time and  $\Delta\nu_R \approx 6 \text{ cm}^{-1}$  is the line width of the Raman shifted line related to the SRS-promoting vibration transition, see also Fig. 5), the corresponding Raman gain coefficient  $g_{ssR}^{St1}$  for the first Stokes generation at  $\lambda_{St1} = 1.0812 \mu\text{m}$  wavelength of the oriented PbB<sub>4</sub>O<sub>7</sub> crystal could roughly be determined. For this estimation we referred to the sufficiently tested method (see, e.g. [21]) based on the well known ratio [22]  $g_{ssR}^{St1} I_p^{thr} l_{SRS} \approx 30$  and a comparative measurement of the “threshold” pump intensity ( $I_p^{thr}$ ) of the confidently detectable first-Stokes lasing signals of lead tetraborate and the reference crystal PbWO<sub>4</sub> ( $\lambda_{St1} = 1.1770 \mu\text{m}$  wavelength [23]) under similar excitation conditions. We found that the measured threshold for PbB<sub>4</sub>O<sub>7</sub> is five to six times higher than that of the tungstate crystal. This results in a value of the  $g_{ssR}^{St1}$  coefficient not less than  $0.5 \text{ cm GW}^{-1}$ .

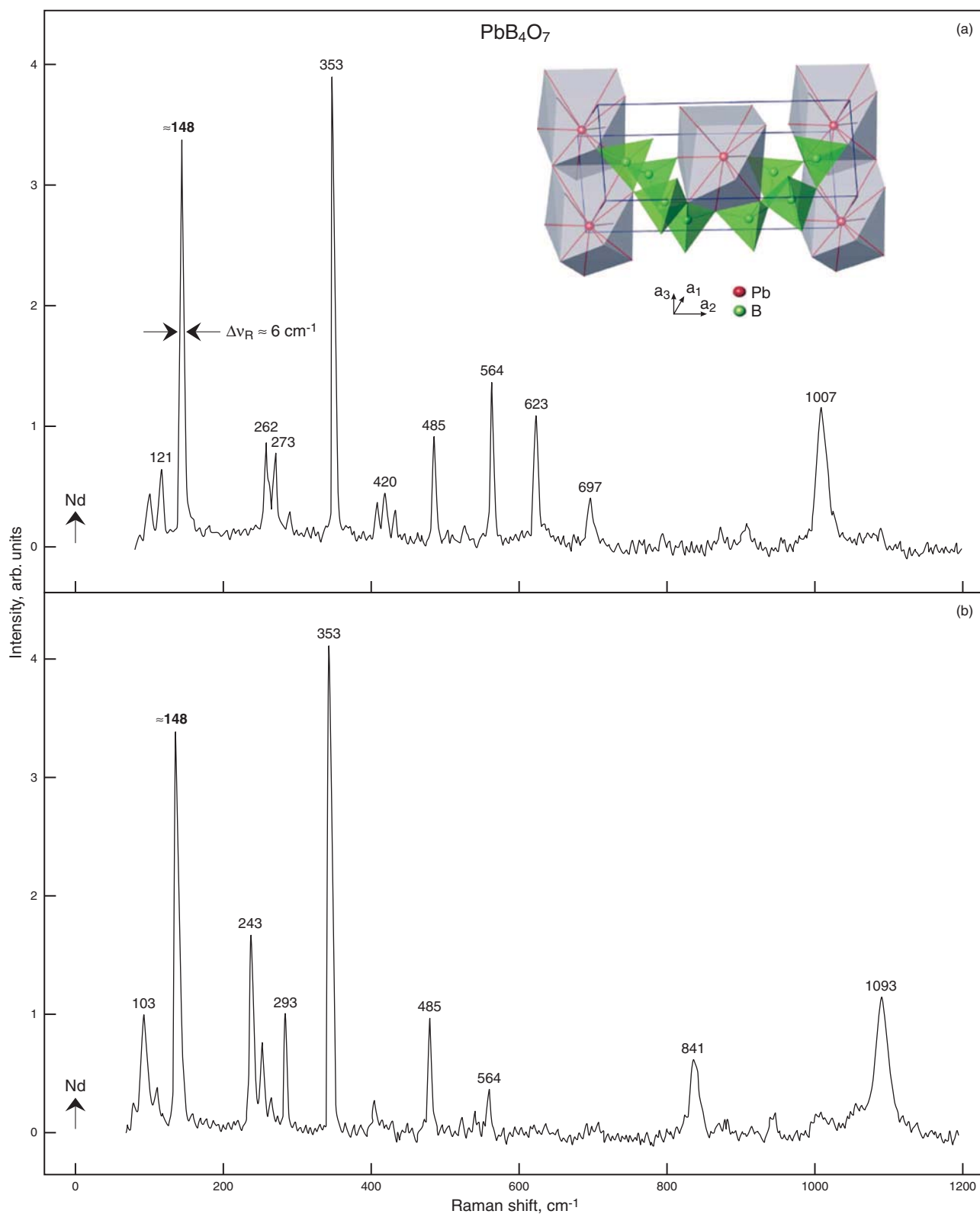
The orthorhombic (primitive) unit cell of the PbB<sub>4</sub>O<sub>7</sub> crystal with space group symmetry  $C_{2v}^7$  contains 24 atoms that have  $3NZ = 72$  degrees of freedom (in Brillouin-zone center at  $\mathbf{k} = 0$ ) described by the irreducible representation:  $\Gamma_{72} = 19A_1 + 17A_2 + 17B_1 + 19B_2$ . Among them  $A_1 + B_1 + B_2$  are the acoustic modes;  $7A_1 + 7A_2 + 6B_1 + 7B_2$  are the lattice translational modes of the B<sup>3+</sup> and



**Figure 3** (online color at [www.lphys.org](http://www.lphys.org)) Room-temperature transmission spectrum in the range from UV to the mid-IR and wavelength dispersion of refractive indices (data from [10]) of an orthorhombic  $\text{Pb}_4\text{O}_7$  single crystal



**Figure 4** Room-temperature SRS, RFWM and cascaded  $\chi^{(3)} \rightarrow \chi^{(2)}$  spectrum of an orthorhombic single crystal of  $\text{Pb}_4\text{O}_7$  recorded in excitation geometry  $c(qq)c$  (with  $\mathbf{q} \parallel (\mathbf{e}_1 + \mathbf{e}_2)$ ) under pumping at  $\lambda_f = 1.06415 \mu\text{m}$  wavelength of  $\text{Nd}^{3+}:\text{Y}_3\text{Al}_5\text{O}_{12}$  picosecond laser.  $\chi^{(3)}$ - and  $\chi^{(2)}$ -lasing lines related to the SRS-promoting vibration  $\omega_{\text{SRS}} \approx 148 \text{ cm}^{-1}$  are indicated by horizontal brackets



**Figure 5** (online color at [www.lphys.org](http://www.lphys.org)) Room-temperature polarized spontaneous Raman scattering  $A_1$ -spectra of the orthorhombic  $\text{Pb}_4\text{O}_7$  single crystal for two excitation geometries: (a) –  $c(aa)c$  and (b) –  $c(bb)c$ . The frequency of some Raman shifted lines are given in  $\text{cm}^{-1}$ . By arrows indicated excitation  $\text{Nd}^{3+}:\text{Y}_3\text{Al}_5\text{O}_{12}$  laser line at  $1.06415 \mu\text{m}$  wavelength. The inset in (a) presents a sketch of the unit cell of  $\text{Pb}_4\text{O}_7$

$\text{Pb}^{3+}$  ions;  $11A_1 + 10A_2 + 10B_1 + 11B_2$  are the internal modes involving the oxygen atoms. The  $A_1$ ,  $B_1$ , and  $B_2$  modes are IR- and Raman-active but  $A_2$  modes are Raman-active only [24]. It means that  $A_1$ ,  $B_1$ , and  $B_2$  modes exhibit polar nature and TO-LO splitting could be determined from these spectra. From the full set of polarized Raman spectra (obtained using Bruker FT100/S spectrometer with CW one-micron  $\text{Nd}^{3+}:\text{Y}_3\text{Al}_5\text{O}_{12}$  pumping laser) of an oriented  $\text{PbB}_4\text{O}_7$  crystalline sample Fig. 5 shows two  $A_1$ -spectra which are recorded in excitation geometries that are close to the pumping condition used for the recording of the cascaded lasing ( $\chi^{(3)} \rightarrow \chi^{(2)}$ )-spectra spectra showed in Fig. 4. The wave numbers of the peaks of the two spectra of spontaneous Raman scattering with their tentative assignment to the respective normal modes are listed in Table 4.

Some features that can be concluded from the conducted Raman measurements are:

- 1) The lattice vibrations below  $200 \text{ cm}^{-1}$  correspond to the  $\text{Pb}^{2+}$  cations translation. Their energy is significantly lower than that of the corresponding vibrations of lithium and sodium tetraborates (see, e.g. [25]) where the lighter cations  $\text{Li}^+$  and  $\text{Na}^+$  appear. The translation of the significantly lighter  $\text{B}^{3+}$  cations contributes the vibration observed in the range  $400\text{--}500 \text{ cm}^{-1}$ ;
- 2) Among the modes observed in the  $A_1$  Raman spectra (in Fig. 5 and as well in further spectra that are not presented here) the strongest lines at  $353$ ,  $\approx 148$ , and  $105 \text{ cm}^{-1}$  could be  $\chi^{(3)}$ -promoting vibration modes. In our SRS experiments we observed  $\omega_{\text{SRS}} \approx 148 \text{ cm}^{-1}$ , only.

## 4. Conclusion

With the obtained results of nonlinear-laser and spectroscopic experiments on the SRS-active non-centrosymmetric  $\text{PbB}_4\text{O}_7$  borate our knowledge on cascaded lasing  $\chi^{(3)} \rightarrow \chi^{(2)}$  processes in nonlinear optical crystals is enhanced to a new structure type. The  $\text{PbB}_4\text{O}_7$  crystal is of special interest for studies of cascaded  $\chi^{(3)} \rightarrow \chi^{(2)}$  processes due to its rather high SHG coefficients with the lack of phase matching.

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